

Measurement of particle momentum (from curvature of its path in a magnetic field)

A particle of charge q travelling at right-angles to a magnetic field B with a speed v experiences a force Bqv at right angles to its motion.

This makes the particle follow a circular path of radius r and the motion is described by

$$Bqv = mv^2/r \rightarrow p = (Bq) r$$

This tells us that for a fixed field B , and charge q , the momentum p is proportional to the radius of curvature r . Here, nature has been kind: all charged particles that live long enough to travel a measurable distance have a charge equal or opposite to the charge on the electron $e = 1.6 \times 10^{-19}$ C.

In units used by nuclear and particle physicists, the relation $p = Bqr$ becomes $p = 0.3r$, where p is measured in GeV/c, B in tesla (T) and r in metres.

For the CERN 2 metre bubble chamber, B was 1.78 T ; for the Fermilab 15-foot bubble chamber, it was 3 T . (At the magnetic north pole, the magnetic field at the earth's surface is 6.2×10^{-5} T .)

Exercise Show, using $p = 0.3Br$, that a particle of momentum 1 GeV/c, moving in the Fermilab 15-foot bubble chamber, has a track with a radius of curvature of about 1 metre.